

Some Stronger Forms of $g^{\mu} b$ –continuous Functions

M.TRINITA PRICILLA * and I.AROCKIARANI * *

*Department of Mathematics, Jansons Institute of Technology
Karumathampatti, India

**Department of Mathematics, Nirmala College for Women,
Coimbatore – 641 046.

Abstract:

The purpose of this paper is to introduce new classes of functions called strongly $g^{\mu} b$ –closed map, strongly $g^{\mu} b$ –continuous, perfectly $g^{\mu} b$ –continuous and strongly $g^{\mu} b$ –irresolute functions in supra topological spaces. Some properties and several characterizations of these types of functions are obtained. Also we investigate the relationship between these classes of functions.

1. Introduction

In 1970, Levine [7] introduced the concept of generalized closed sets in topological spaces and a class of topological spaces called $T_{1/2}$ spaces. Extensive research on generalizing closedness was done in recent years by many Mathematicians [4,5,7,8,9]. Andrijevic[2] introduced a new class of generalized open sets in a topological space, the so-called b -open sets. In 1983, A.S.Mashhour et al [9] introduced the notion of supra topological spaces and studied S - S continuous functions and S^* – continuous functions. In 2010, O.R.Sayed and Takashi Noiri [12] introduced supra b – open sets and supra b – continuity on topological spaces. In 2011, I.Arockiarani and M.Trinita Pricilla[3] introduced a new class of generalized b -open sets in supra topological spaces.

In this paper we introduce and investigate notions of new classes of functions namely strongly g^{μ} –closed, strongly $g^{\mu} b$ –closed, strongly g^{μ} –continuous, strongly $g^{\mu} b$ –continuous, strongly g^{μ} –irresolute, strongly $g^{\mu} b$ –irresolute, almost g^{μ} –irresolute and almost $g^{\mu} b$ –irresolute functions in supra topological spaces. Relations between these types of functions and other classes of functions are obtained. We also note that the class of $g^{\mu} b$ –closed map is properly placed between strongly $g^{\mu} b$ –closed map and almost $g^{\mu} b$ –closed map.

2. Preliminaries

Definition: 2.1 [9]

A subclass $\tau^* \subset P(X)$ is called a supra topology on X if $X \in \tau^*$ and τ^* is closed under arbitrary union. (X, τ^*) is called a supra topological space (or supra space). The members of τ^* are called supra open sets.

Definition: 2.2 [9]

The supra closure of a set A is defined as $Cl^{\mu}(A) = \cap \{B : B \text{ is supra closed and } A \subseteq B\}$

The supra interior of a set A is defined as $Int^{\mu}(A) = \cup \{B : B \text{ is supra open and } A \supseteq B\}$

Definition 2.3 [12]

Let (X, μ) be a supra topological space. A set A is called a supra b – open set if $A \subseteq Cl^{\mu}(Int^{\mu}(A)) \cup Int^{\mu}(Cl^{\mu}(A))$. The complement of a supra b – open set is called a supra b – closed set.

Definition: 2.4 [3]

Let (X, μ) be a supra topological space. A set A of X is called supra generalized – closed set (simply g^{μ} – closed) if $cl^{\mu}(A) \subseteq U$ whenever $A \subseteq U$ and U is supra open. The complement of supra generalized – closed set is supra generalized – open set.

Definition: 2.5 [3]

Let (X, μ) be a supra topological space. A set A of X is called supra generalized b – closed set (simply $g^{\mu} b$ – closed) if $bcl^{\mu}(A) \subseteq U$ whenever $A \subseteq U$ and U is supra open. The complement of supra generalized b – closed set is supra generalized b – open set.

Definition: 2.6 [14]

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be $g^{\mu} b$ –continuous if $f^{-1}(V)$ is $g^{\mu} b$ – closed in (X, τ) for every supra closed set V of (Y, σ) .

Definition: 2.7 [14]

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be $g^{\mu} b$ –irresolute if $f^{-1}(V)$ is $g^{\mu} b$ – closed in (X, τ) for every $g^{\mu} b$ – closed set V of (Y, σ) .

Definition :2.8 [16]

A supra topological space (X, μ) is said to be supra $T_{g^{\mu}b}$ -space if every $g^{\mu}b$ -closed set is b^{μ} - closed.

Definition : 2.9 [16]

A supra topological space (X, μ) is said to be supra T_g -space if every $g^{\mu}b$ -closed set is g^{μ} - closed.

Definition: 2.10 [13]

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called *Perfectly $^{\mu}$ continuous* if $f^{-1}(V)$ is $cl^{\mu}open^{\mu}$ in X for each supra open set V of Y .

Definition: 2.11 [15]

A Subset A of (X, μ) is said to be supra regular open if $A = Int^{\mu}(Cl^{\mu}(A))$ and supra regular closed if $A = cl^{\mu}(Int^{\mu}(A))$.

Definition : 2.12[14]

A map $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be $g^{\mu}b$ -closed map if for every supra closed F of X , $f(F)$ is $g^{\mu}b$ -closed in Y .

3. Strongly $g^{\mu}b$ -closed map

Definition: 3.1

A map $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly g^{μ} -closed map if for every g^{μ} -closed F of X , $f(F)$ is g^{μ} -closed in Y .

Definition: 3.2

A map $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly $g^{\mu}b$ -closed map if for every $g^{\mu}b$ -closed F of X , $f(F)$ is $g^{\mu}b$ -closed in Y .

Theorem: 3.3

(i) If $f : (X, \tau) \rightarrow (Y, \sigma)$ is $g^{\mu}b$ -closed map and $g : (Y, \sigma) \rightarrow (Z, \gamma)$ is strongly $g^{\mu}b$ -closed map then $g \circ f : (X, \tau) \rightarrow (Z, \gamma)$ is $g^{\mu}b$ -closed map.

(ii) If $f : (X, \tau) \rightarrow (Y, \sigma)$ is supra-closed map and $g : (Y, \sigma) \rightarrow (Z, \gamma)$ is strongly $g^{\mu}b$ -closed map then $g \circ f : (X, \tau) \rightarrow (Z, \gamma)$ is $g^{\mu}b$ -closed map.

Proof: It is obvious.

Remark: 3.4

If $f : (X, \tau) \rightarrow (Y, \sigma)$ is strongly $g^{\mu}b$ -closed map and $g : (Y, \sigma) \rightarrow (Z, \gamma)$ is supra closed map then the composite map $g \circ f$ may not be strongly $g^{\mu}b$ -closed map and it is shown by the following example.

Example: 3.5

Let $X = \{a, b, c\}$, $\tau = \{\emptyset, X, \{a\}\} = \sigma$, $\eta = \{\emptyset, X, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. Let $f : (X, \tau) \rightarrow (X, \sigma)$ and $g : (X, \sigma) \rightarrow (X, \eta)$ be an identity map. Then f is strongly $g^{\mu}b$ -closed map and g is supra closed map but $(g \circ f)\{b\} = \{b\}$ is not $g^{\mu}b$ -closed in (X, η) . Therefore $g \circ f$ is not strongly $g^{\mu}b$ -closed map.

Definition: 3.6

A map $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be almost $g^{\mu}b$ -closed map if for every *regular $^{\mu}$* closed F of X , $f(F)$ is $g^{\mu}b$ -closed in Y .

Theorem: 3.7

- (i) Every strongly $g^{\mu}b$ -closed map is almost $g^{\mu}b$ -closed map.
- (ii) Every strongly $g^{\mu}b$ -closed map is $g^{\mu}b$ -closed map.

(iii) Every g^{μ} b-closed map is almost g^{μ} b-closed map.

Proof: It is obvious.

Remark: 3.8

The converse of the above theorem is not true and it is shown by the following examples.

Example: 3.9

Let $X = \{a, b, c, d\}$, $\tau = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}$. Let $f : (X, \tau) \rightarrow (X, \tau)$ be defined by $f(a) = c; f(b) = a; f(c) = d; f(d) = b$. Here f is almost g^{μ} b-closed but not strongly g^{μ} b-closed map.

Example: 3.10

Let $X = \{a, b, c, d\}$, $\tau = \{\phi, X, \{a\}, \{c\}, \{a, c\}\}$. Let $f : (X, \tau) \rightarrow (X, \tau)$ be defined by $f(a) = b; f(b) = a; f(c) = d; f(d) = c$. Here f is almost g^{μ} b-closed but $f\{b, d\} = \{a, c\}$ is not g^{μ} b-closed. Therefore f is not g^{μ} b-closed map.

Theorem: 3.11

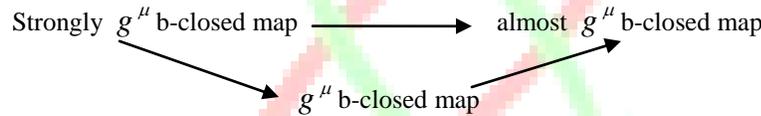
If $f : (X, \tau) \rightarrow (Y, \sigma)$ is almost g^{μ} b-closed map and $g : (Y, \sigma) \rightarrow (Z, \gamma)$ is strongly g^{μ} b-closed map then $g \circ f : (X, \tau) \rightarrow (Z, \gamma)$ is almost g^{μ} b-closed map.

Proof: It is obvious.

Theorem: 3.12

The composite mapping of two strongly g^{μ} b-closed map is strongly g^{μ} b-closed map.

From the above theorem and example we have the following diagram



4. Strongly g^{μ} b-continuous and perfectly g^{μ} b-continuous maps

Definition: 4.1

A function $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly g^{μ} b-continuous if the inverse image of every g^{μ} b-open set of Y is supra open in (X, τ) .

Definition: 4.2

A function $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly g^{μ} b-continuous if the inverse image of every g^{μ} b-open set of Y is supra open in (X, τ) .

Theorem: 4.3

(i) Every strongly g^{μ} b-continuous function is supra-continuous.

(ii) Every strongly g^{μ} b-continuous function is strongly g^{μ} b-continuous

The converse of the above theorem is not true and it is shown by the following example

Example: 4.4

Let $X = \{a, b, c\}$; $\tau = \{\phi, X, \{a\}\}$ and $\sigma = \{\phi, X, \{a\}, \{c\}, \{a, c\}\}$. Define $f : (X, \tau) \rightarrow (X, \sigma)$ by $f(a) = a, f(b) = c$ and $f(c) = b$. Then f is supra continuous but $f^{-1}\{a\} = \{a\}$ is not supra closed. Therefore f is not strongly g^{μ} b-continuous.

Theorem: 4.5

If $f : (X, \tau) \rightarrow (Y, \sigma)$ is strongly g^{μ} b-continuous and $g : (Y, \sigma) \rightarrow (Z, \gamma)$ is g^{μ} b-continuous then $g \circ f : (X, \tau) \rightarrow (Z, \gamma)$ is supra continuous.

Definition: 4.6

A function $f : (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} b-continuous if the inverse image of every g^{μ} b-open set of Y is $cl^{\mu} open^{\mu}$ in (X, τ) .

Definition: 4.7

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} b-continuous if the inverse image of every g^{μ} b-open set of Y is $cl^{\mu} open^{\mu}$ in (X, τ) .

Theorem: 4.8

- (i) If a function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} b-continuous function then f is perfectly g^{μ} continuous.
- (ii) If a function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} b-continuous function then f is strongly g^{μ} b-continuous.
- (iii) If a function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} -continuous function then f is perfectly g^{μ} continuous.
- (iv) If a function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} -continuous function then f is strongly g^{μ} -continuous.
- (v) If a function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be perfectly g^{μ} b-continuous function then f is perfectly g^{μ} -continuous .

Example: 4.9

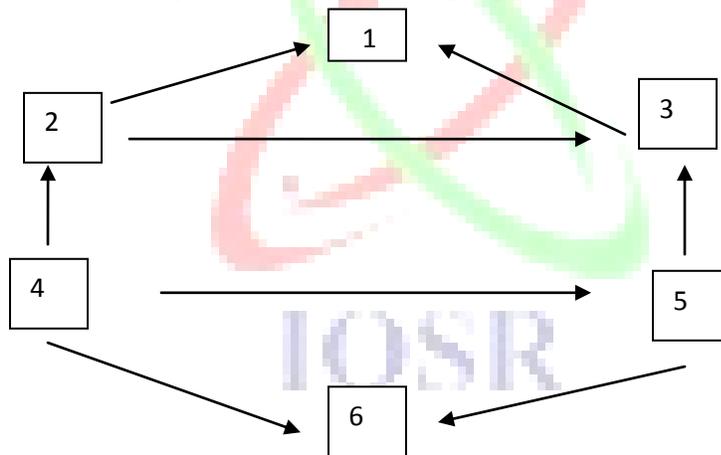
Let $X = \{a, b, c\}$; $\tau = \{\emptyset, X, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$ and $\sigma = \{\emptyset, X, \{a\}\}$. Define $f: (X, \tau) \rightarrow (X, \sigma)$ be an identity map. Then f is perfectly g^{μ} continuous but it is not perfectly g^{μ} -continuous and perfectly g^{μ} b-continuous.

Theorem: 4.10

If $f: (X, \tau) \rightarrow (Y, \sigma)$ is perfectly g^{μ} continuous and if Y is both $T_{\frac{1}{2}}^{\mu}$ -space and T_{gb}^{μ} -space, then f is perfectly g^{μ} b-continuous.

From the above theorem and examples we have the following implications:

From the above theorem and examples we have the following implications:



Here the numbers 1-5 represent the following:

- 1. Supra continuous
- 2. strongly g^{μ} b-continuous
- 3. strongly g^{μ} -continuous
- 4. Perfectly g^{μ} b-continuous
- 5. Perfectly g^{μ} -continuous
- 6. Perfectly g^{μ} -continuous

5. Strongly g^{μ} b -irresolute and Almost g^{μ} b-irresolute Functions

Definition: 5.1

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly g^{μ} -irresolute if $f^{-1}(V)$ is supra open in (X, τ) for every g^{μ} -open set V of (Y, σ) .

Definition: 5.2

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly g^{μ} b-irresolute if $f^{-1}(V)$ is supra open in (X, τ) for every g^{μ} b-open set V of (Y, σ) .

Theorem: 5.3

- (i) Every strongly g^{μ} b-irresolute function is g^{μ} b-irresolute.

- (ii) Every strongly g^{μ} b-irresolute function is g^{μ} b-continuous.
- (iii) Every strongly g^{μ} -irresolute function is g^{μ} -irresolute.
- (iv) Every g^{μ} b-irresolute function is g^{μ} b-continuous.

Proof: (i) Let V be g^{μ} b-open in (Y, σ) . Since f is strongly g^{μ} b-irresolute, $f^{-1}(V)$ is supra open in (X, τ) and hence it is g^{μ} b-open in (X, τ) . Therefore f is g^{μ} b-irresolute.

Remark: 5.4

The converses of the above theorems are not true and it is shown by the following examples.

Example: 5.5

- (i) Let $X = \{a, b, c\}$; $\tau = \{\phi, X, \{a\}\}$ and $\sigma = \{\phi, X, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. Define $f: (X, \tau) \rightarrow (X, \sigma)$ by $f(a) = b, f(b) = a$ and $f(c) = c$. Then f is g^{μ} b-irresolute. But $f^{-1}\{a\} = \{b\}$ is not supra closed. Therefore f is not strongly g^{μ} b-irresolute.
- (ii) Let $X = \{a, b, c, d\}$; $\tau = \{\phi, X, \{a\}, \{c\}, \{a, c\}\}$ and $\sigma = \{\phi, X, \{a\}\}$. Define $f: (X, \tau) \rightarrow (X, \sigma)$ be an identity function. Here f is g^{μ} b-continuous. But $f^{-1}\{a, c\} = \{a, c\}$ is not g^{μ} b-closed. Therefore f is not strongly g^{μ} b-irresolute.

Definition: 5.6

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be strongly b^{μ} -irresolute if $f^{-1}(V)$ is supra open in (X, τ) for every b^{μ} -open set V of (Y, σ) .

Theorem: 5.7

- (i) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is strongly b^{μ} -irresolute and Y is $T_{gb^{\mu}}$ -space then f is strongly g^{μ} b-irresolute.
- (ii) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is strongly g^{μ} -irresolute and Y is $T_{g^{\mu}}$ -space then f is strongly g^{μ} b-irresolute.

Proof: It is obvious.

Theorem: 5.8

- (i) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is strongly g^{μ} b-irresolute function then f is strongly b^{μ} -irresolute.
- (ii) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is strongly g^{μ} b-irresolute function then it is strongly g^{μ} -irresolute.

Proof: It is obvious.

Remark: 5.9

The converse of the above theorem is not true and it is shown by the following example.

Example: 5.10

Let $X = \{a, b, c\}$; $\tau = \{\phi, X, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$ and $\sigma = \{\phi, X, \{a\}\}$. Define $f: (X, \tau) \rightarrow (X, \sigma)$ by $f(a) = b, f(b) = a, f(c) = c$. Then f is strongly b^{μ} -irresolute. But $f^{-1}\{c\} = \{c\}$ is not supra open in (X, τ) . Therefore f is not strongly g^{μ} b-irresolute.

Example: 5.11

Let $X = \{a, b, c\}$; $\tau = \{\phi, X, \{a\}, \{c\}, \{a, c\}\}$. Let $f: (X, \tau) \rightarrow (X, \tau)$ be an identity function. Here f is strongly g^{μ} -irresolute. But $f^{-1}\{a\} = \{a\}$ is not supra closed in (X, τ) . Therefore f is not strongly g^{μ} b-irresolute.

Theorem: 5.12

For a function $f: (X, \tau) \rightarrow (Y, \sigma)$ if f is strongly g^{μ} b-irresolute then for each $x \in X$ and each g^{μ} b-open set V of Y containing $f(x)$ there exist a supra open set U of X containing x such that $f(U) \subset V$.

Proof: Let $x \in X$ and V be any g^{μ} b-open set V of Y containing $f(x)$. since f is strongly g^{μ} b-irresolute then $f^{-1}(V)$ is supra open in X and contains x . Let $U = f^{-1}(V)$ then U is supra open subset of X containing x such that $f(U) \subset V$.

Theorem: 5.13

Let $f: (X, \tau) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \gamma)$ be any two functions then the composition $g \circ f: (X, \tau) \rightarrow (Z, \gamma)$ is i) strongly g^{μ} b-irresolute if f is strongly g^{μ} b-irresolute and g is g^{μ} b-irresolute

(ii) g^u b-irresolute if f is g^u b-continuous and g is strongly g^u b-irresolute.

Proof: It is obvious.

Definition: 5.14

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is almost g^u -irresolute if $f^{-1}(V)$ is b^u -open in (X, τ) for every g^u -open set V of (Y, σ) .

Definition: 5.15

A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is almost g^u b-irresolute if $f^{-1}(V)$ is b^u -open in (X, τ) for every g^u b-open set V of (Y, σ) .

Theorem: 5.16

- (i) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is almost g^u b-irresolute then it is b^u -continuous map.
- (ii) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is almost g^u b-irresolute then it is g^u b-irresolute map.
- (iii) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is almost g^u -irresolute then it is b^u -continuous map.
- (iv) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is almost g^u b-irresolute then it is almost g^u -irresolute map.
- (v) If $f: (X, \tau) \rightarrow (Y, \sigma)$ is b^u -continuous then it is g^u b-continuous map.

Proof: (i) Let V be supra open in (Y, σ) and hence g^u b-open set in (Y, σ) . Since f is almost g^u b-irresolute $f^{-1}(V)$ is b^u -open in (X, τ) . Hence f is b^u -continuous.

Remark: 5.17

The converse of the above theorem is not true and it is shown by the following examples.

Example: 5.18

Let $X = \{a, b, c, d\}$; $\tau = \{\emptyset, X, \{a\}, \{b\}, \{a, b\}\}$. Define $f: (X, \tau) \rightarrow (X, \tau)$ be an identity function. Here f is b^u -continuous. But $f^{-1}\{a, b, c\} = \{a, b, c\}$ is not b^u -closed. Therefore f is not almost g^u b-irresolute.

Example: 5.19

Let $X = \{a, b, c\}$; $\tau = \{\emptyset, X, \{a\}\}$ and $\sigma = \{\emptyset, X, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. Define $f: (X, \tau) \rightarrow (X, \sigma)$ by $f(a) = b, f(b) = a, f(c) = c$. Hence f is g^u b-irresolute. But $f^{-1}\{b, c\} = \{a, c\}$ is not b^u -closed. Therefore f is not almost g^u b-irresolute.

Theorem: 5.20

- Let $f: (X, \tau) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \gamma)$ be any two functions then the composition $g \circ f: (X, \tau) \rightarrow (Z, \gamma)$ is
- (i) almost g^u b-irresolute if f is almost g^u b-irresolute and g is g^u b-irresolute
 - (ii) almost g^u b-irresolute if f is b^u -irresolute and g is almost g^u b-irresolute.

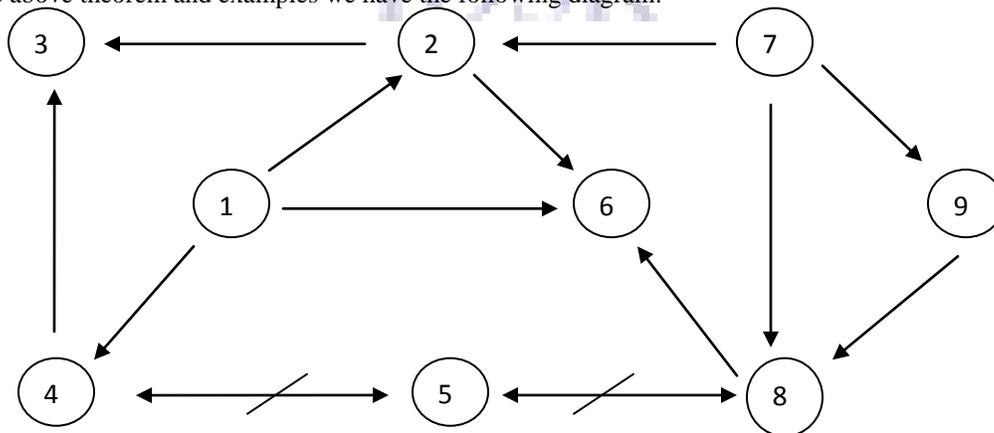
Proof: It is obvious.

Theorem: 5.21

For a function $f: (X, \tau) \rightarrow (Y, \sigma)$ if f is almost g^u b-irresolute then for each $x \in X$ and each g^u b-open set V of Y containing $f(x)$ there exist a supra open set U of X containing x such that $f(U) \subset V$.

Proof: It is obvious.

From the above theorem and examples we have the following diagram:



Here the numbers 1-9 represent the following implication:

1. Strongly g^u b-irresolute 2. g^u b-irresolute 3. g^u -irresolute

4. Strongly g^{μ} -irresolute 5. Strongly b^{μ} -irresolute 6. g^{μ} b-continuous
 7. almost g^{μ} b-irresolute 8. b^{μ} -continuous 9. almost g^{μ} -irresolute

References:

- [1] M.E. Abd El – Monsef, S.N. El – Deeb and R.A. Mahmoud, β -open sets and β - continuous mappings. *Bull. Fac. Sci. Assiut Univ.*, 12 (1983), 77-90.
 [2] D.Andrijevic, on b-open sets, *Mat. Vesnik* 48(1996),no.1-2,59-64.
 [3] I. Arockiarani and M.Trinita Pricilla, On Supra generalized b-closed sets, *Antarctica Journal of Mathematics*, Volume 8(2011).
 [4] S.P.Arya and T.M.Nour, characreizations of s-normal spaces, *Indian J.Pure Appl.Math.*21(1990),no.8,717-719.
 [5] J.Dontchev, On generalizing semi-preopen sets, *Mem.Fac.Sci.Kochi Univ.Ser.A.Math.*16(1995),35-48.
 [6] E.Ekici and M.Caldas, Slightly continuous functions, *bol.Soc.Parana.Mat.*(3)22(2004),no.2, 63-74 .
 [7] N.Levine, Generalized closed sets in topology, *Rend. Circ.Mat.Palermo*(2)19(1970),89-96.
 [8] H.Maki, R.Devi and K.Balachandran, Associated topologies of generalized α -closed sets and α -generalized closed sets, *Mem. Fac.Sci.Kochi Univ.Ser.A.Math.*15(1994),51-63.
 [9] A.S. Mashhour, A.A. Allam, F.S. Mahamoud and F.H.Khedr, On supra topological spaces, *Indian J.Pure and Appl. Math. No. 4, 14* (1983), 502 – 510.
 [10] Mahmoud, R.A. and M.E.Abd El-Monsef, 1990, β –irresolute and β –topological invariant, *Proc.Pakistan Acad.Sci.*,27(No.3):285-296.
 [11] Nasef, A.A. and Noiri, T. 1997. Some weak forms of almost continuity, *Acta Math Hungar*, 74:211
 [12] O.R. Sayed and Takashi Noiri, on supra b - open sets and supra b - continuity on topological spaces, *European Journal of pure and applied Mathematics*, 3(2) (2010), 295 – 302.
 [13] M.Trinita Pricilla and I. Arockiarani, on almost contra $g^{\mu} b$ –continuous functions, *International Journal of Mathematical sciences and Applications*.(To Appear)
 [14] M.Trinita Pricilla and I. Arockiarani, $g^{\mu} b$ - Homeomorphisms in Supra Topological spaces *International Journal of Mathematical Sciences and Engineering Applications*.(To Appear)
 [15] M.Trinita Pricilla and I. Arockiarani, ”on supra T-closed sets”, *International journal of Mathematical Archive*,2(8)(2011)1-5.
 [16] I. Arockiarani and M.Trinita Pricilla, approximately - $g^{\mu} b$ - continuous maps in supra topological spaces, *Kerala Mathematical Association*.(To Appear)
 [17] Veerakumar, M.K.R.S. 2000. Between closed sets and g-closed sets, *Mem.Fac.Sci.Kochi Univ.(Math)*21:1-19