Stress Distribution in Soils under Pile Cap of Tapered Piles in Compressible Clay

T.W. Adejumo

Abstract: This research paper presents the results of comprehensive investigations on stress distribution in soils under pile cap of tapered piles in compressible clay. Compressible clay from Urucha and Shabani, area of Minsk province, Belarus was investigated in this work. The former was used for laboratory investigation, while field tests were conducted on the latter respectively. The results show the influence of axial compressive load on the magnitude, pattern and orientation of stresses in soils under the pile cap of loaded modeled instrumental piles bored into compressive clay soil. Stresses in the soils at different depths under the pile cap with reference to pile center lines were measured and compared with those obtained using Boussinesq’ theory. Measured stresses are slightly higher than those calculated using the theory. The investigations also showed that, for tapered piles bored in compressive clay, the stress increases towards the center line of pile-pile cap joint irrespective of tapering angle only up to 0.5m below the cap, (model), beyond this point, the magnitude and pattern of stress changes. The vertical normal stress under the pile cap increases from zero at the surface to 42% in depth lower than 3.5R, and 55% beyond this point. The maximum principal stress is directed along the radius vector R and reduces radially outward from the pile centerline. The normal and shear stress vectors are less in pile with higher center to center spacing. In addition, stress distribution under pile cap is also a function of pile spacing and tapering angle. Clearly striated stressed zones of deformation under loaded pile cap, having depth in multiples of pile diameter were observed.

Keywords: Compressible clay, Deformation, Settlement, Stress in soil, Tapered pile

I. INTRODUCTION

As foundation engineers, a significant amount of the work we do is based on the concept of stress. Stress analysis allows us to obtain the normal and shear stresses in any plane passing through a point, given the normal and shear stresses acting on mutually perpendicular planes passing through the point [1]. When pile is penetrates in a downward frictional mode, a failure zone is developed along the soil-pile interface which partly upheaves laterally and disturbs the soil below the pile tip. Partly consolidation develops around soil-pile interface when soil compresses elastically below the critical depth [2].

The pile cap is defined as a structural member used to distribute the load to the piles [3]. The flexibility of the pile cap affects individual pile head forces significantly and affects the bending moments and shear forces in individual piles as well, even though the displacement of the pile cap does not vary much [4]. When the pile cap distributes an equal magnitude of load on each pile, the following assumptions must be satisfied according to Bowles: (a) the pile cap is in contact with the ground, (b) the piles are all vertical, (c) a load is applied at center of pile group, and (d) the pile group is symmetrical [3].

Investigations and data on measured stress in clay are limited, and even the available few are mostly for compacted clays. There is almost no convenient way of inserting a load cell into natural (undisturbed) clay without causing severe stress redistribution problems. A variety of laboratory tests as well as field techniques are available, each having its own limitations as well as advantages [5]. Equations for the stresses and strains induced in a homogeneous, isotropic, weightless, linearly elastic half space, with a plane horizontal surface, by a point load perpendicular to the surface and acting at the surface, was first solved in usable form by Boussinesq [6] & [7], and later by Acum and Fox [8], with a few others in between. Foster and Fergus obtained information on the spatial variation in developed pressure in compacted clay. They concluded that Boussinesq’s theory is adequately accurate, at least for compacted clays [9]. Solutions for the stress and deformation caused by a vertical point load applied at the surface have been presented by Koning [10] and Barber [11]. Biot established an equation for determination of normal stress in rigid floor [12]. Cummings worked further on Biot’s equations to determine the vertical normal stress on the base directly beneath the center of a uniformly loaded disc [13]. The lateral deformation of piles decreases with increase in distance from the pile center line, while outward radial deformations recorded around the pile decreases downwards along the length [14]. The skin friction and radial stress are highly influenced by tapered piles compared with conventional piles. The tapering and wedging
effects are responsible for increase in normalized skin friction and normalized lateral stresses. Taper-shaped piles offer a larger resistance than the cylindrical piles [2] and [15].

Although the assumptions are usually made that the soil is homogeneous and isotropic, it is apparent that most field problems involve soils that are stratified and anisotropic [16]. Based on the strength of their digenetic bonds, clay and clay-shale have been grouped into 3: 1) over consolidated plastic clay with weak or no bond; 2) over consolidated plastic clay with well-developed digenetic bonds and c) over consolidated plastic clay with strongly-developed digenetic bonds [17]. Clay soils around Minsk region falls into the third category [18]-[20]. In spite of these results however, more work still needed to be done for greater understanding of the dynamics of pile-soil or pile cap-soil behavior under stress.

The object of this paper therefore, is to present the results of a series of modeled pile tests on stress distribution under the pile cap of tapered piles conducted in the research laboratory, Geotechnical and Environmental Engineering department, Belarusian National Technical University, Minsk, and field tests on the outskirts of Minsk province, Belarus. This investigation is essential in the understanding of structural behavior of the soil under axially loaded pile cap of tapered piles, and its response to loading. Obtaining the stress distribution of soil immediately the below the piles cap under loads is a key factor to understanding its behavior and response to deformation and utmost functionality. The foregoing therefore, explains the relevance of this investigation.

II. MATERIALS AND METHOD

The materials and method employed in this work can simply be divided into; a) theoretical determination of the stress exerted on the soil using Boussinesq equation, b) laboratory investigations for the model tapered piles, c) field tests with bored tapered piles having pile cap in contact with the soil, and d) analysis of both calculated and measured stress from the controlled tests.

1.1 Theoretical Determination of Stress

Besides the tabulation of Ahlvin and Uleri [21], increase in vertical stress at any point below a rectangular area subjected to uniform load can be calculated using Boussinesq’s solution [22], [16]. For most practical analyses of the settlement behavior of soils, it is assumed that the volume of the soil is controlled exclusively by the vertical stress, $\sigma_z$. Using Boussinesq solution and r-t-z coordinate system, superimposed on the traditional x-y coordinates, the vertical stress in soil under the axially loaded pile cap in Fig. 1 is given by:

$$\sigma_z = \frac{3P}{2\pi R^3} = \frac{3P}{2\pi R^2} \cos^3 \beta = I \frac{P}{Z^2}$$

(1)

Where P is axial load; I is influence factor (ratio of r/z) given by Terzaghi [23] and Taylor [24];

![Fig. 1: Symbols and direction of entities used in the equation for stress under axially loaded pile cap](image-url)

Introducing x-axis in disperses and Poisson’s ratio, the spatial distribution of normal stress and shearing stress is given by the equations:
1.2 Laboratory Investigations

Clay samples tested were taken from a construction site at Urucha, at the outskirt of Minsk, Belarus. The soil was conditioned and detailed laboratory investigation was carried out to determine the stress distribution under the pile cap when modeled tapered piles were bored into it. The test with modeled piles of 20mm diameter and 200mm long was conducted in the test tank shown in Fig. 2, in the post graduate laboratory of the Department of Geotechnics & Civil Engineering, Faculty of Civil Engineering, Belarusian National University, Minsk, Belarus. A detailed, easy-to-follow procedure on this has been covered in my earlier works; Adejumo et al [25] and Adejumo [26]. Test results were collected and collated for further analysis.

1.3 Field Investigations

The field tests were performed on 4 No 320mm diameter tapered piles with tapering angles (α) of 1.43° and 0.95°, and group efficiency of 0.85 and 0.95 at two test points respectively, at a construction site in Shabani industrial layout, on the outskirt of Minsk. The pile cap configuration was 2260 X 2260 X 500mm in dimension. Static loads were applied and maintained using a hydraulic jack (of 200T capacity) and were measured with a load cell as shown in Fig. 3. Reaction to the jack load is provided by a steel frame that is attached to an array of steel H-piles located at least 1.5m away from the test piles. Pile cap settlements were measured relative to a fixed reference beam using 2 dial gauges. Displacement/settlement of soils around the piles measurements were made in reference to the pile cap using 5 dial gauges, Fig. 4. The settlements were recorded for each loading increment at an interval of 15 minutes or the time when the movement of the indicator on the dial gauges becomes insignificant. The modeled test piles were instrumented with strain gauges connected to the stylishly perforated steel cone-heads by string-pulley (for static resistance) with censors to the pile centerline. The steel cone-heads with series of springs connected to the indicators were installed in the soils around the piles at depths 0.2m, 0.5m, 1.0m 1.5m, and the 5th one at 0.2m outside the pile cap. The piles were subjected to axial compressive loads until the allowable pile settlement of 0.1d (10% of pile diameter) is reached or exceeded in line with the submission of [27-29]. The vertical normal stress and deformation during loading and unloading were then recorded.
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Fig. 2: Testing tank for laboratory investigations

Fig. 3: Loading device for field investigations (200Tonnes capacity)

Fig. 4: Dial guages for sensor movement measurement under pile cap
III. RESULTS AND DISCUSSION

The results of geotechnical properties of the compressive clay investigated in the laboratory is presented in Table 1 below. It shows a high void ration (e) and cohesion with maximum values of 1.92 and 30 kPa respectively, which indicated the compressibility of the sample. It does not drain readily and may absorb water by capillary action, which lead to loss of strength.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values for the Sample</th>
<th>High void ratio (e) and cohesion (kPa) indicate the compressibility of the clay sample</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density (γ, kN/m³)</td>
<td>18</td>
<td></td>
</tr>
<tr>
<td>Moisture content (w)</td>
<td>10</td>
<td></td>
</tr>
<tr>
<td>Specific gravity of solids</td>
<td>2.63</td>
<td></td>
</tr>
<tr>
<td>Liquid Limit (%)</td>
<td>23 - 29</td>
<td></td>
</tr>
<tr>
<td>Plastic Limit (%)</td>
<td>17 - 19</td>
<td></td>
</tr>
<tr>
<td>Plasticity index (%)</td>
<td>5 - 10</td>
<td></td>
</tr>
<tr>
<td>Liquidity Index (%)</td>
<td>0.1 - 0.3</td>
<td></td>
</tr>
<tr>
<td>Void ratio (e)</td>
<td>0.70 - 1.92</td>
<td></td>
</tr>
<tr>
<td>Cohesion (kPa)</td>
<td>25 - 30</td>
<td></td>
</tr>
<tr>
<td>Angle of internal friction (φ°)</td>
<td>7 - 18</td>
<td></td>
</tr>
<tr>
<td>Modulus of Deformation E (kPa)</td>
<td>7.5 - 13</td>
<td></td>
</tr>
</tbody>
</table>

The result of theoretical (calculated) stress is shown in Table 2. Using the r-t-z coordinate system, with the normal stress equal to the radius vector R at equilibrium, the maximum vertical shear stress beyond which the soil experiences yield is 7.03 kPa. Table 3 shows the normal and shear stress measured during loading and unloading. It shows slightly higher shear stress value of 7.39 kPa for the corresponding load. The vector correlation coefficient of r = 0.922 was obtained for the calculated and the experimental stress.

<table>
<thead>
<tr>
<th>Load (kPa)</th>
<th>0.00</th>
<th>0.50</th>
<th>1.00</th>
<th>1.50</th>
<th>2.00</th>
<th>2.50</th>
<th>3.00</th>
</tr>
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<tbody>
<tr>
<td>Stress</td>
<td>σ</td>
<td>τ</td>
<td>σ</td>
<td>τ</td>
<td>σ</td>
<td>τ</td>
<td>σ</td>
</tr>
<tr>
<td>Pile cap</td>
<td>0.00</td>
<td>0.00</td>
<td>0.09</td>
<td>6.47</td>
<td>0.19</td>
<td>6.55</td>
<td>0.29</td>
</tr>
<tr>
<td>0.2m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.09</td>
<td>6.45</td>
<td>0.19</td>
<td>6.56</td>
<td>0.29</td>
</tr>
<tr>
<td>0.5m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.09</td>
<td>6.47</td>
<td>0.20</td>
<td>6.58</td>
<td>0.29</td>
</tr>
<tr>
<td>1.0m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.10</td>
<td>6.48</td>
<td>0.21</td>
<td>6.59</td>
<td>0.30</td>
</tr>
<tr>
<td>1.5m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.11</td>
<td>6.49</td>
<td>0.22</td>
<td>6.60</td>
<td>0.34</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Load (kPa)</th>
<th>0.00</th>
<th>0.50</th>
<th>1.00</th>
<th>1.50</th>
<th>2.00</th>
<th>2.50</th>
<th>3.00</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stress</td>
<td>σ</td>
<td>τ</td>
<td>σ</td>
<td>τ</td>
<td>σ</td>
<td>τ</td>
<td>σ</td>
</tr>
<tr>
<td>Pile cap</td>
<td>0.00</td>
<td>0.00</td>
<td>0.10</td>
<td>6.85</td>
<td>0.19</td>
<td>6.93</td>
<td>0.29</td>
</tr>
<tr>
<td>0.2m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.09</td>
<td>6.83</td>
<td>0.19</td>
<td>6.93</td>
<td>0.29</td>
</tr>
<tr>
<td>0.5m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.10</td>
<td>6.85</td>
<td>0.20</td>
<td>6.94</td>
<td>0.29</td>
</tr>
<tr>
<td>1.0m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.10</td>
<td>6.84</td>
<td>0.21</td>
<td>6.95</td>
<td>0.30</td>
</tr>
<tr>
<td>1.5m</td>
<td>0.00</td>
<td>0.00</td>
<td>0.11</td>
<td>6.86</td>
<td>0.22</td>
<td>6.97</td>
<td>0.34</td>
</tr>
</tbody>
</table>

The Load-settlement curves for the laboratory instrumented tapered piles are shown in Figs. 5 and 6. Soils around tapered piles with higher tapering angle (α) show less settlement (5-10% lower) at the initial period of loading. However, they produced a generally higher settlement and deformations in soils closer to and around the pile tip with a depth of failure tip influence zone 10 times the pile diameter, while those with less tapering
angle is 7.5 times their diameter. Pile cap settlement is 110% and 102% higher than soil settlements around tapered piles with tapering angles of 0.95° and 1.43° respectively.

Vertical and spatial stress along the pile axis under pile cap follow the usual pattern as shown in the failure bulb around an idealized pile of the four in a group of 4-piles in Fig. 7. It also followed the pattern of increasing radially outward from pile center in agreement with the finding of Salgado [30]. Four zones of deformation with depth of 2.5D, 3D, 2.5D, and 2D from pile cap line downward. D is diameter of pile.
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The stress distribution pattern, intensity and magnitude in soil around tapered piles bored into compressive clay soil obtained from sites on the outskirt of Minsk region, when subjected to compressive axial loads investigated in this study have been presented. The results of the investigations showed that in compressive clay, the stress increases towards the center line of pile-pile cap joint of tapered piles irrespective of tapering angle only up to 0.5m below the cap, (same as depth of pile cap itself), beyond this point, the magnitude and pattern of stress changes. The vertical normal stress under the pile cap increases from zero at the surface to 42% in depth lower than 3.5R, and 55% beyond this point. The maximum principal stress is directed along the radius vector R and reduces radially outward from the pile centerline. The shear stress value beyond the radius vector, R is of 7.03 kPa for the calculated/theoretical test, while a higher value 7.39 kPa was obtained on the field. The average depth of failure zone for tapered piles with pile spacing (η) of 0.95, and tapering angle (α) 0.95° is 7.5 times pile diameter, whereas it’s 10 times diameter of piles when the tapering angle is increased to 1.43°. Stress intensity, which is directly proportional to settlement, is also influenced by the tapering angle relative to the diameter of the pile, and this effect increases with incremental depth of pile penetration into compressive clay soil. Pile cap settlement is 5-10% higher in tapered piles with lower tapering angle. While laboratory test revealed soils on the upper layer of tapered piles with higher tapering angle underwent greater stress, the field tests result shows the contrary. Slightly larger confining pressure for the laboratory test as well as induced stress on the field may be responsible for this.

V. ACKNOWLEDGEMENTS

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REFERENCES

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